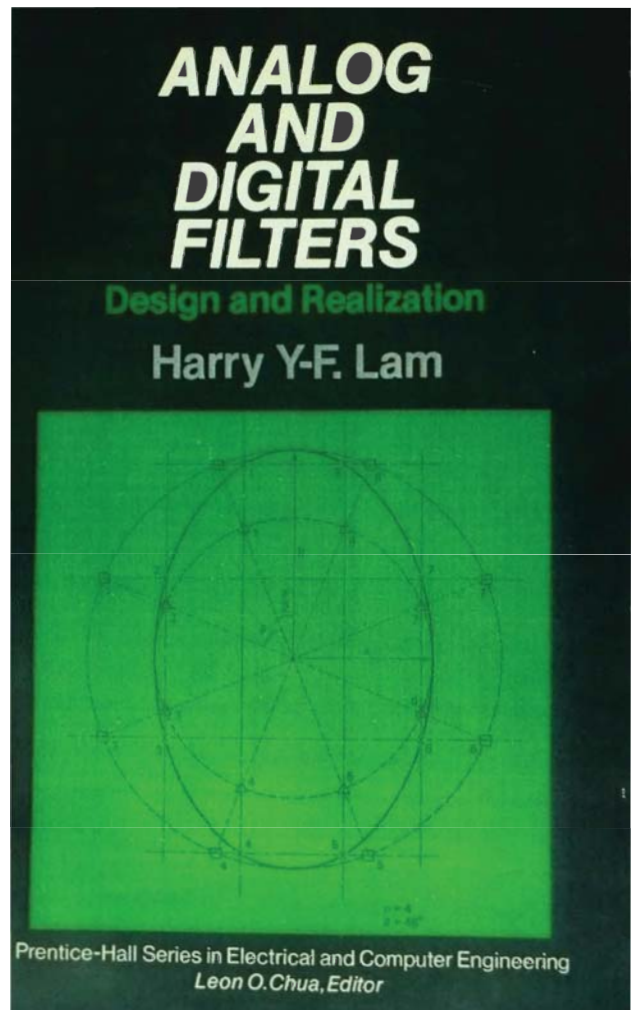


**ANALOG AND
DIGITAL FILTERS:
DESIGN AND REALIZATION**

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