

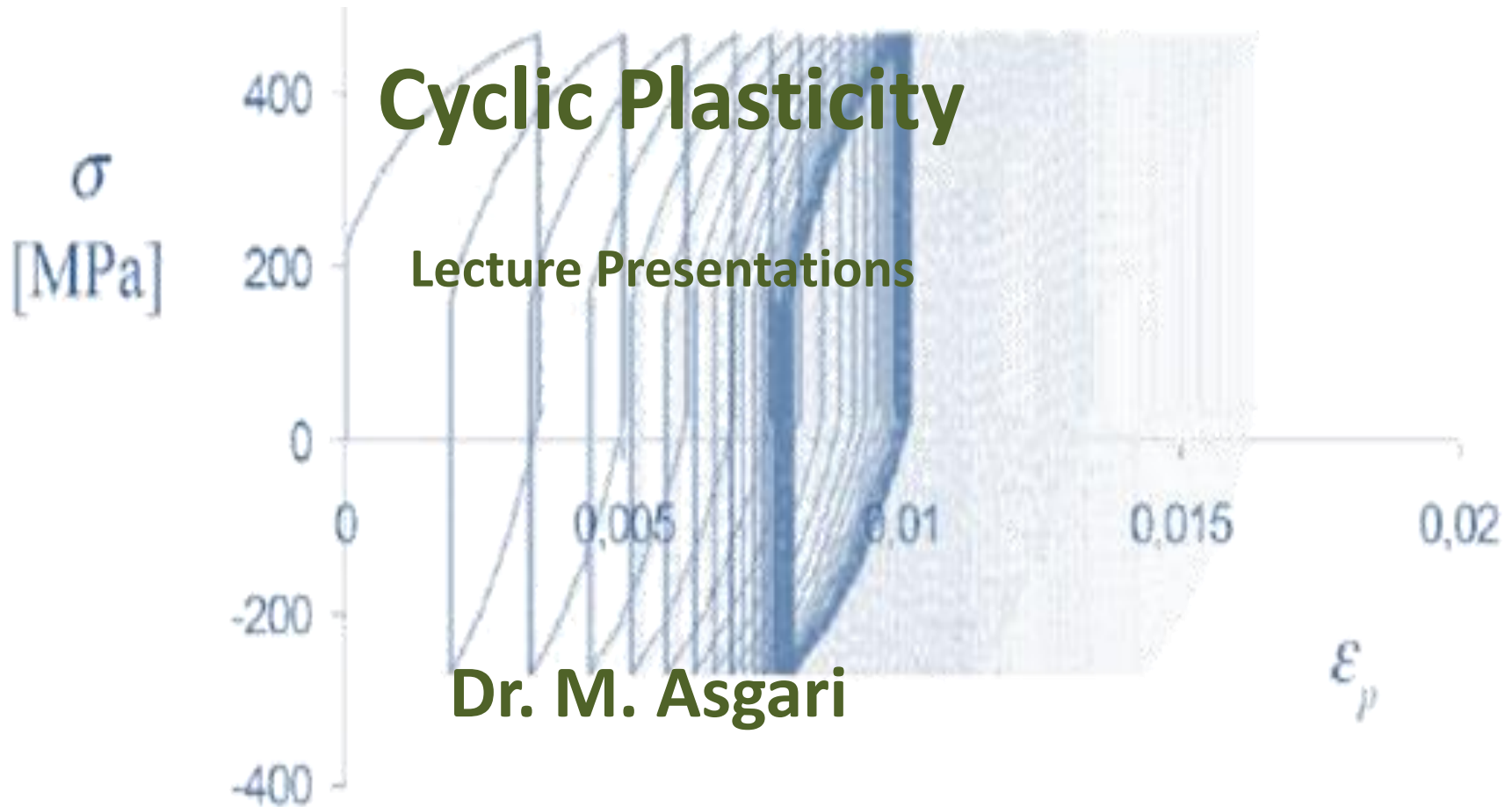
به نام خداوند جان و خرد

کزین برتر اندیشه برنگذرد



دانشگاه صنعتی خواجه نصیرالدین طوسی

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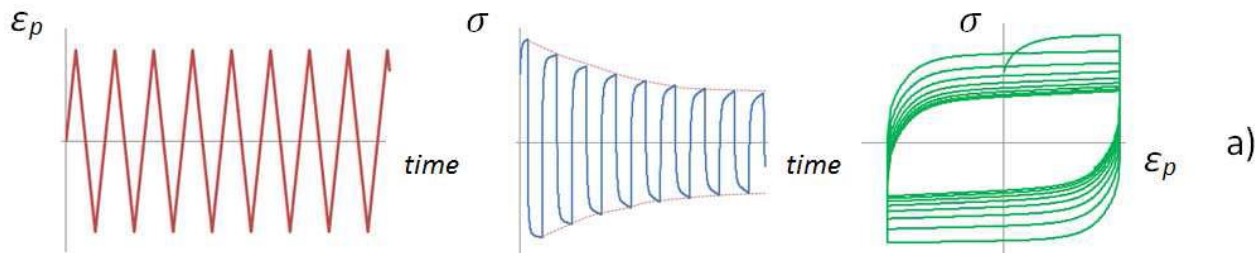


# Cyclic Controlled Loading

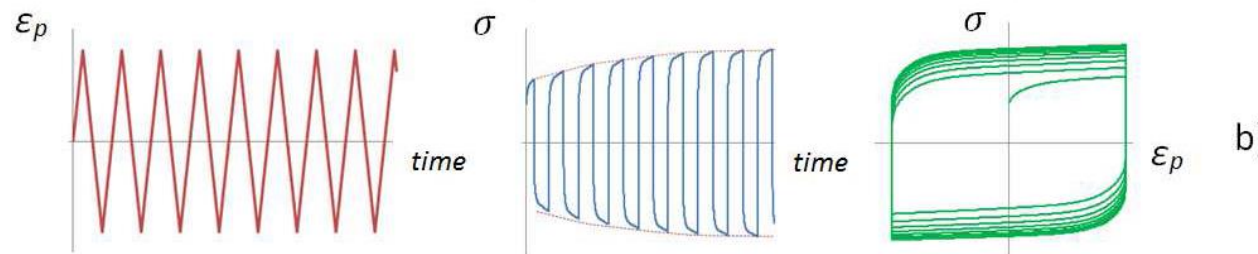
Fig. 1

**strain controlled loading:**

- Cyclic Softening

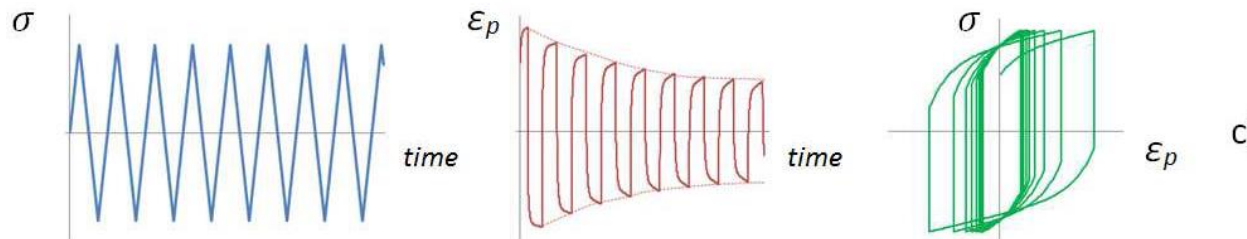


- Cyclic Hardening

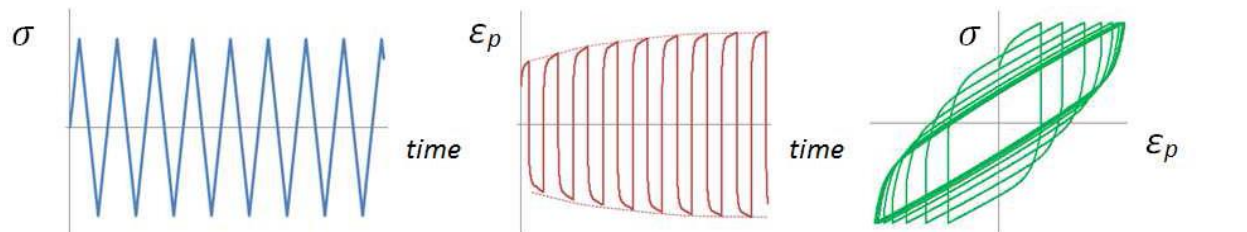


**stress controlled loading:**

- Cyclic Hardening



- Cyclic Softening



## Ratcheting

Scheme of uniaxial ratcheting and influence of hardening/softening behaviour.

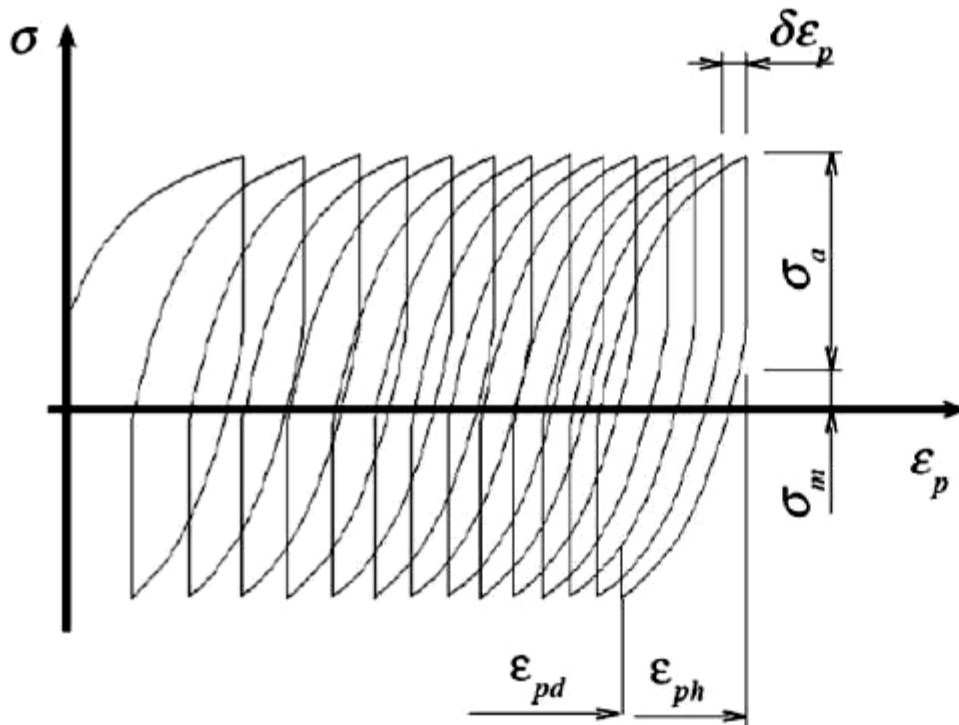


Fig. 2

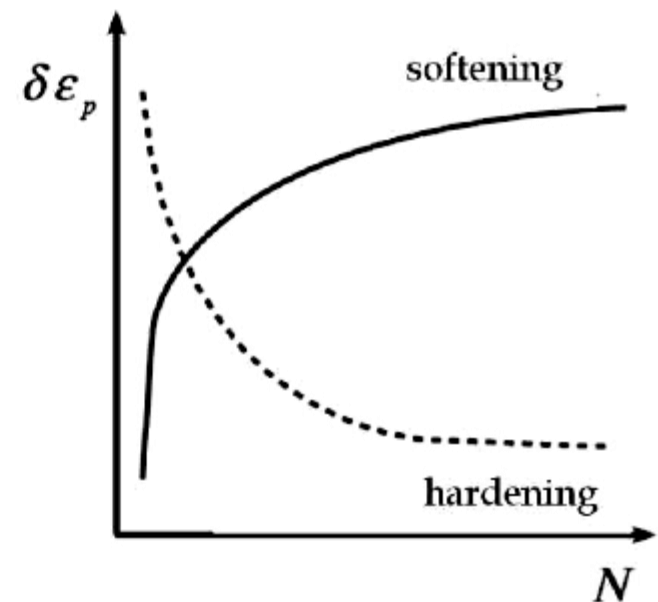


Fig. 3

# Ratcheting and Shakedown

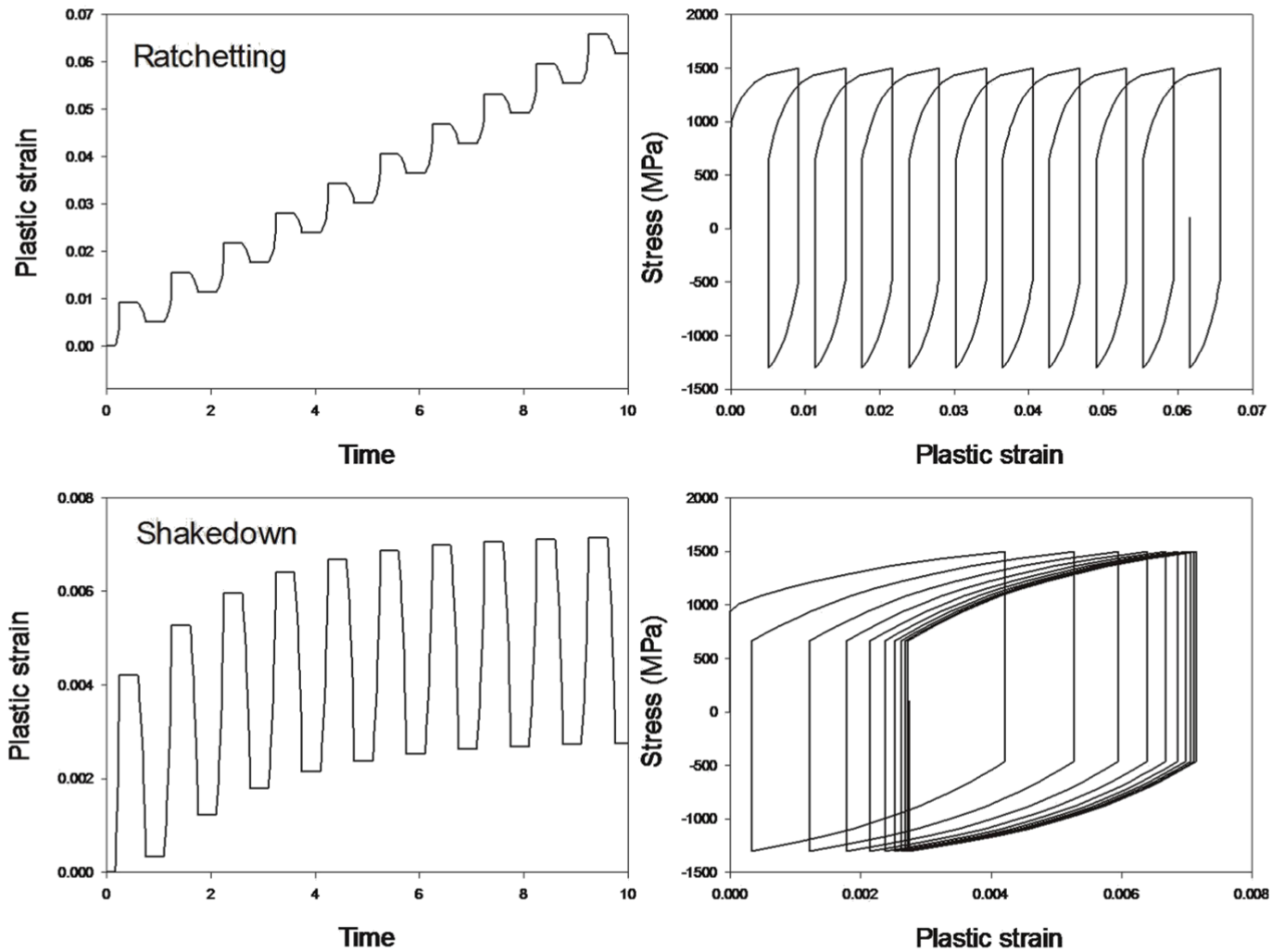


Fig. 4

## Cyclic stress-strain curve of ST52 steel.

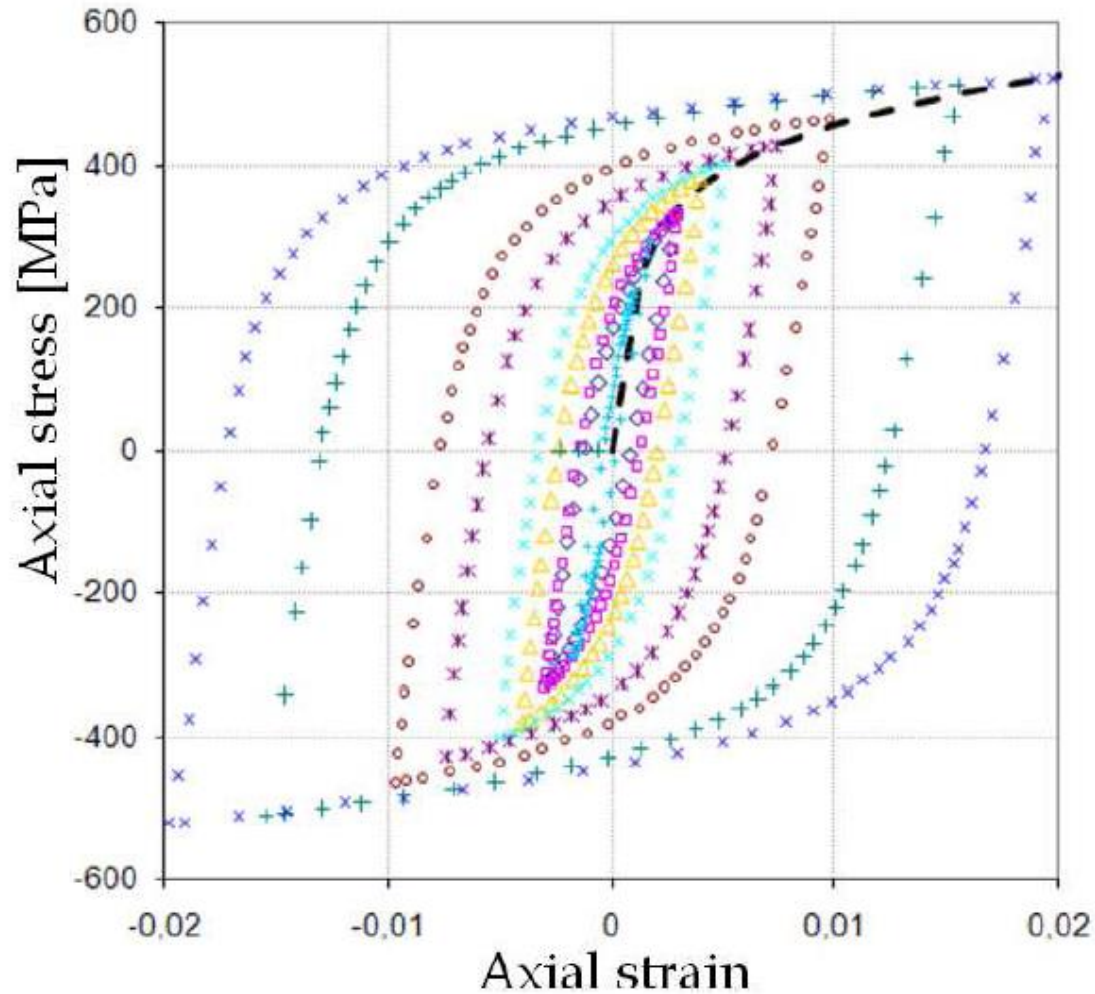


Fig. 5

## Masing Behaviour

representation of Masing Behaviour

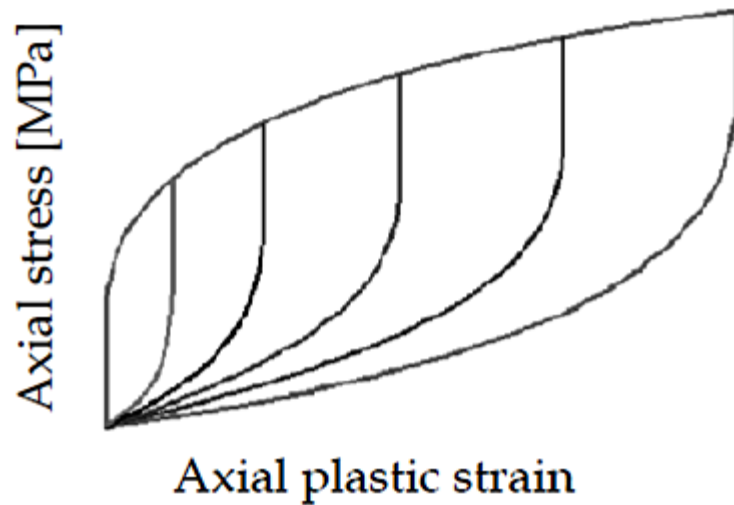


Fig. 6

Non-Masing's Behaviour of ST52 steel

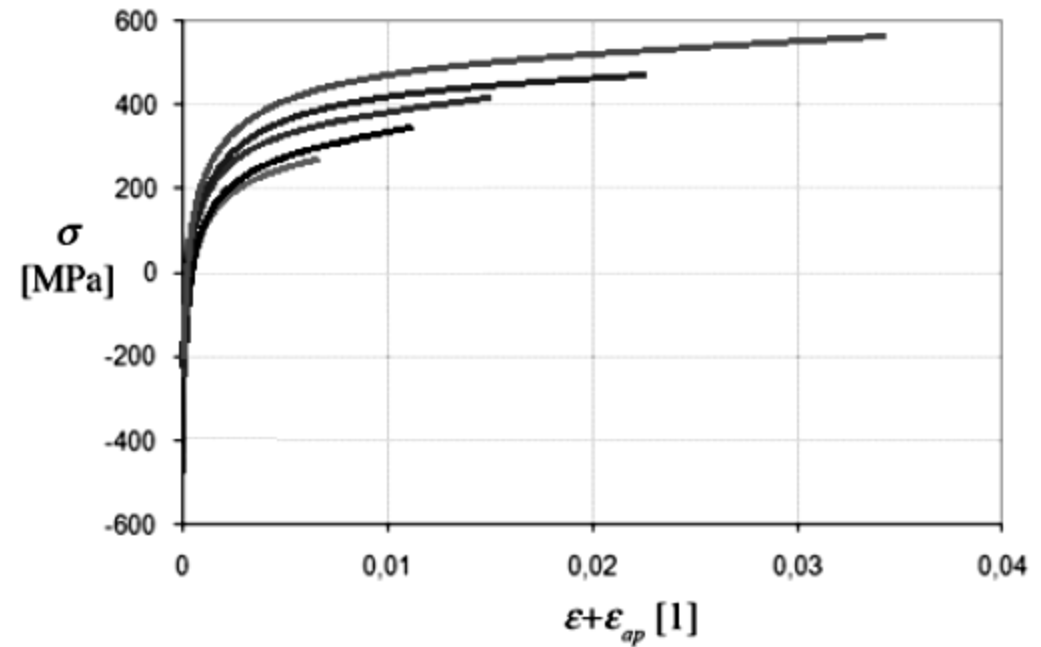


Fig. 7

# Stress Relaxation

## Mean stress relaxation under nonsymmetric strain cycles

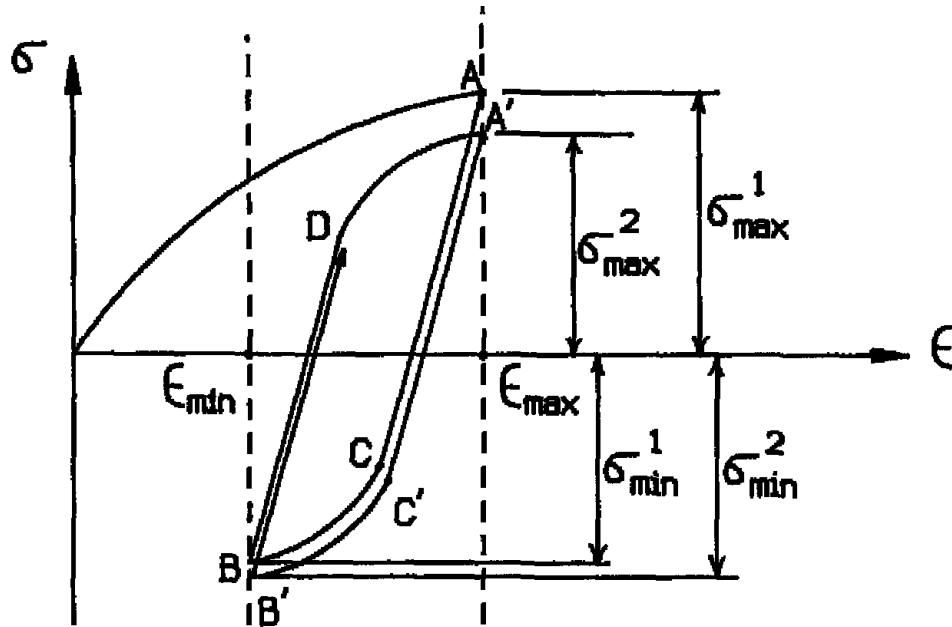
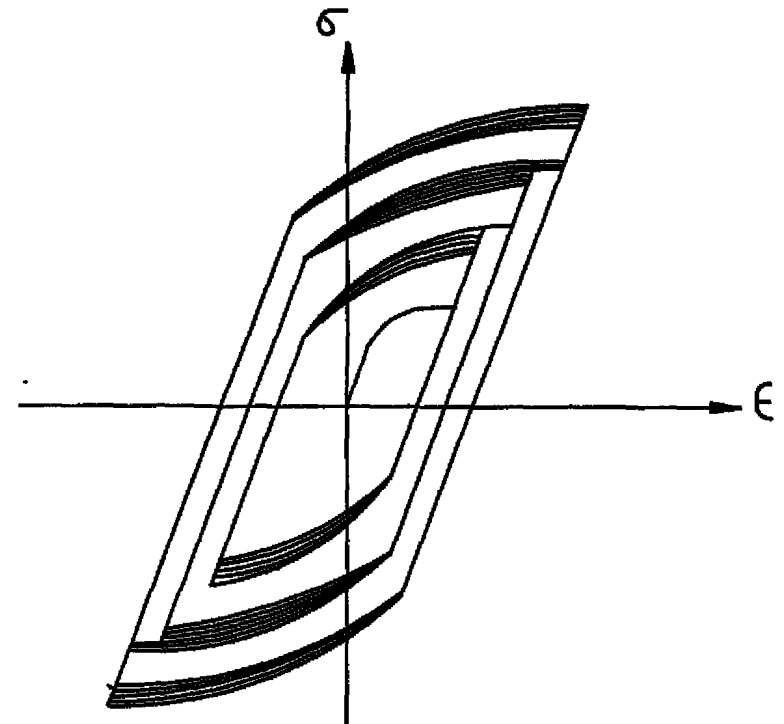


Fig. 8



Controlled strain testing on 316 L steel at 20°C, (Chaboche 1979)

Fig. 9



## mixed hardening

Von Mises yield function with mixed hardening in the deviatoric plane

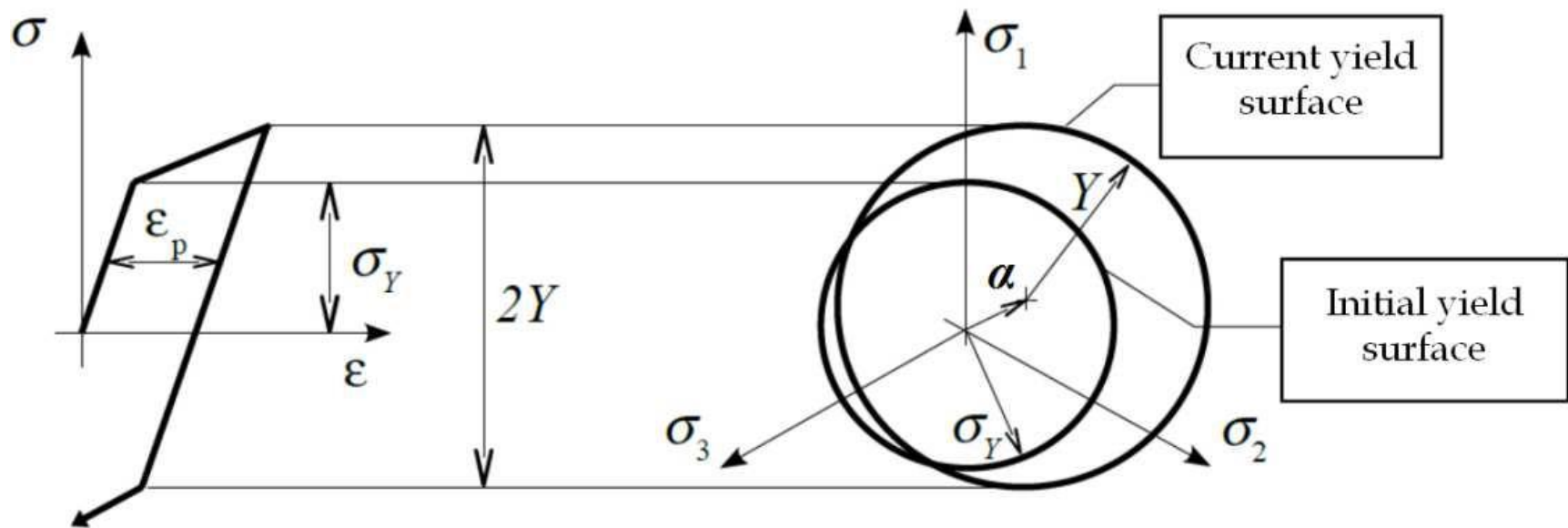


Fig.10

## hardening Models

### Isotropic hardening Model

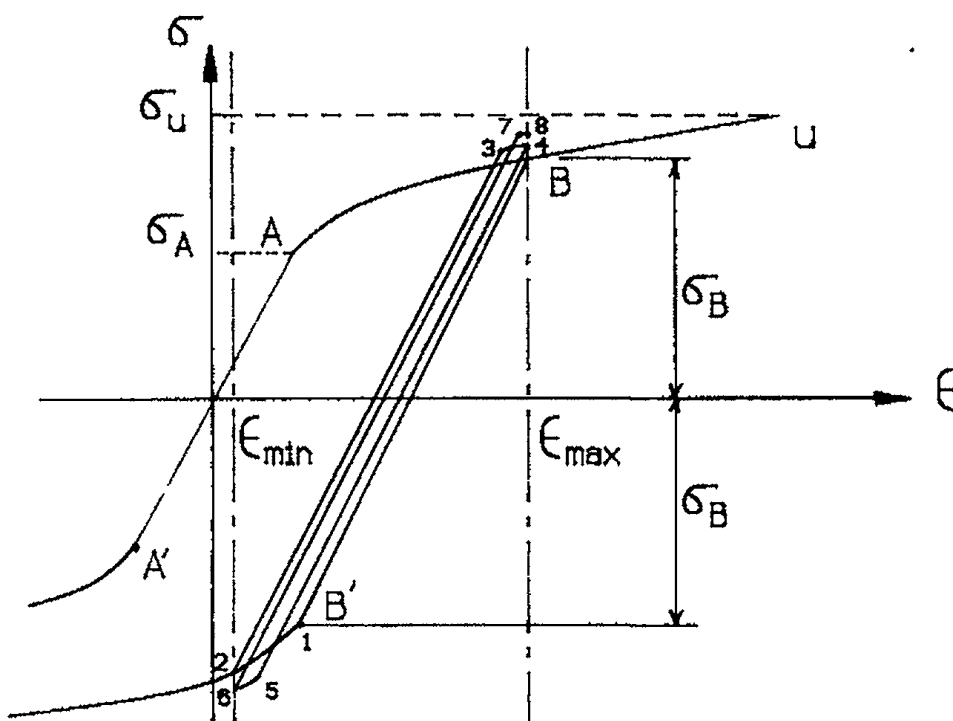


Fig. 11

### Linear Kinematic hardening Model

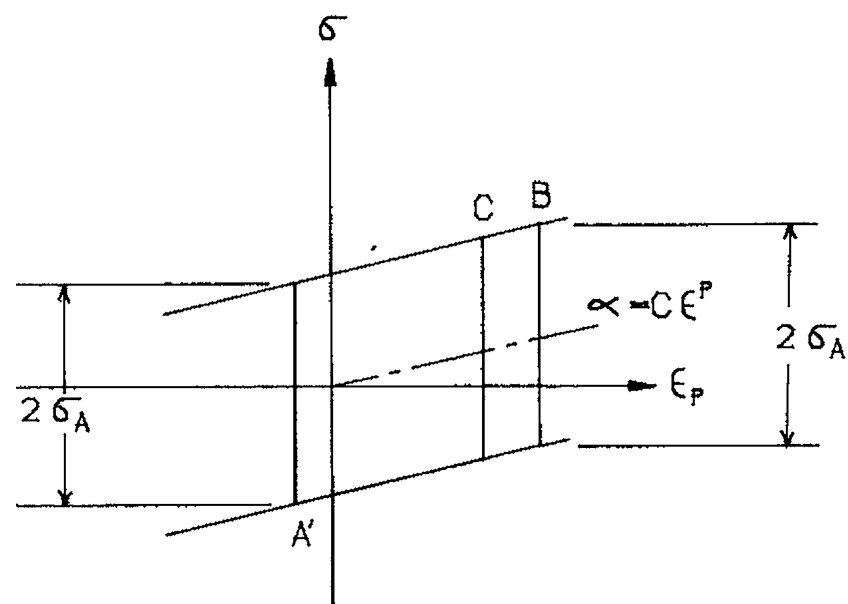


Fig. 12

# hardening Models

Mroz approximation Model

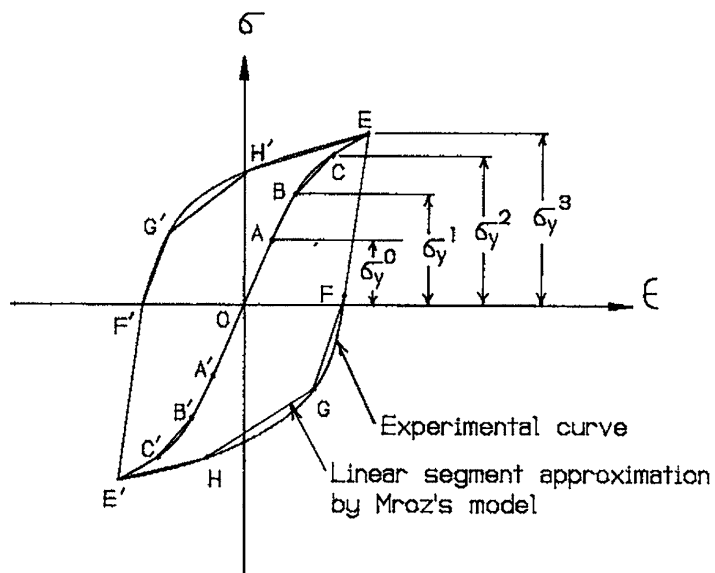


Fig. 13

General Multi-surfaces Model

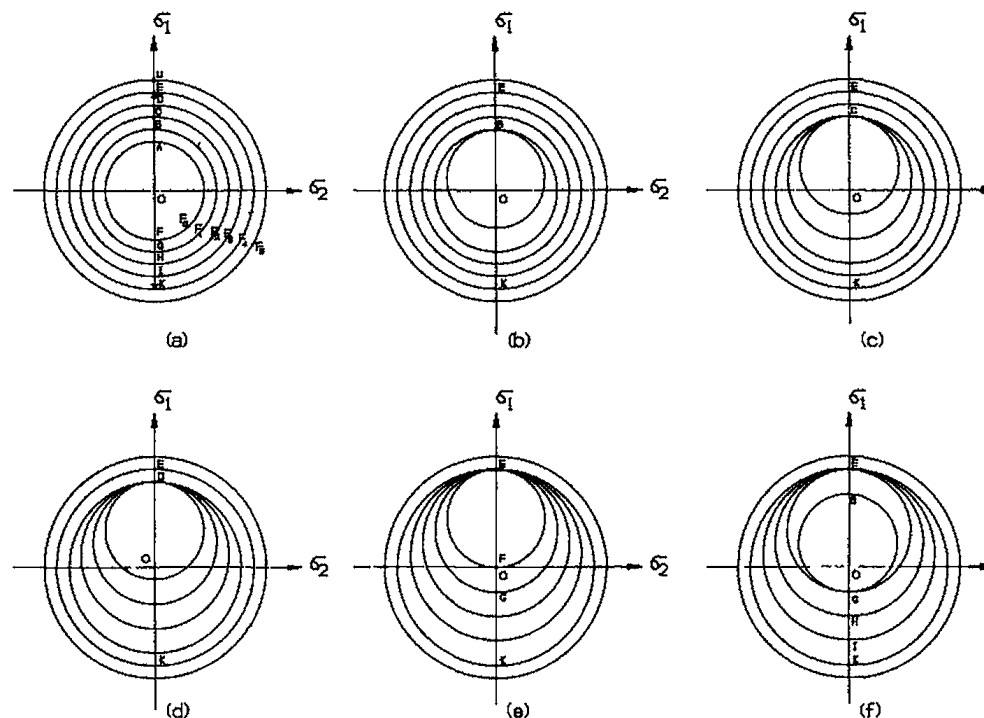


Fig. 14

## hardening Models

nonlinear kinematic hardening model of Armstrong/Frederick

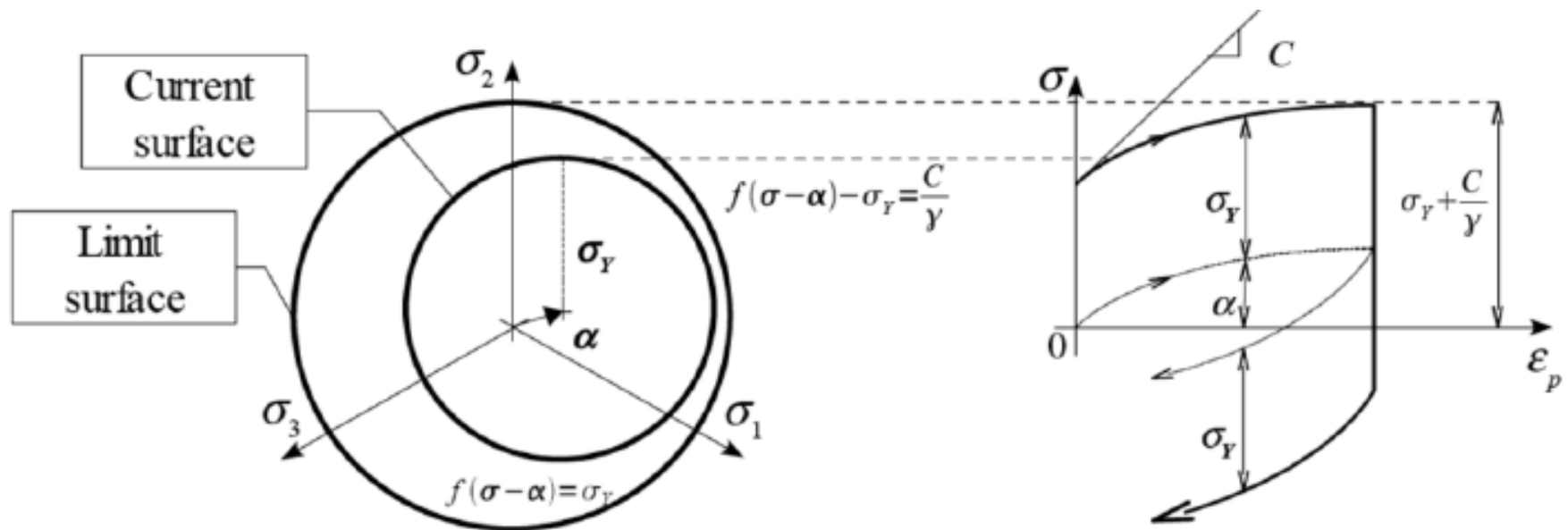


Fig. 15

## hardening Models

hysteresis loop to identify parameters of Chaboche model

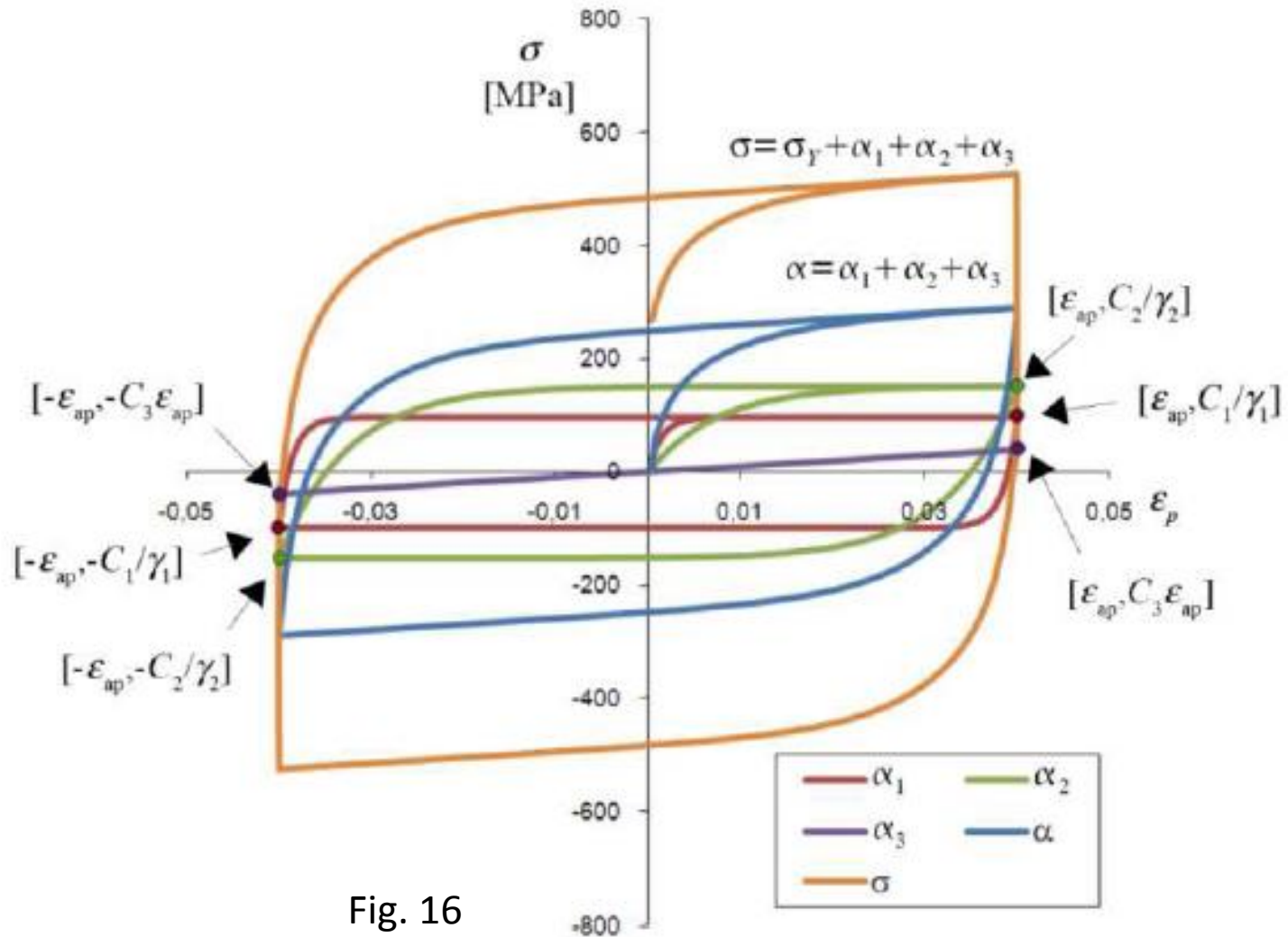


Fig. 16

## hardening Models

Influence of parameter  $\gamma_2$  on ratcheting response of the Chaboche model ( $M=2$ ).

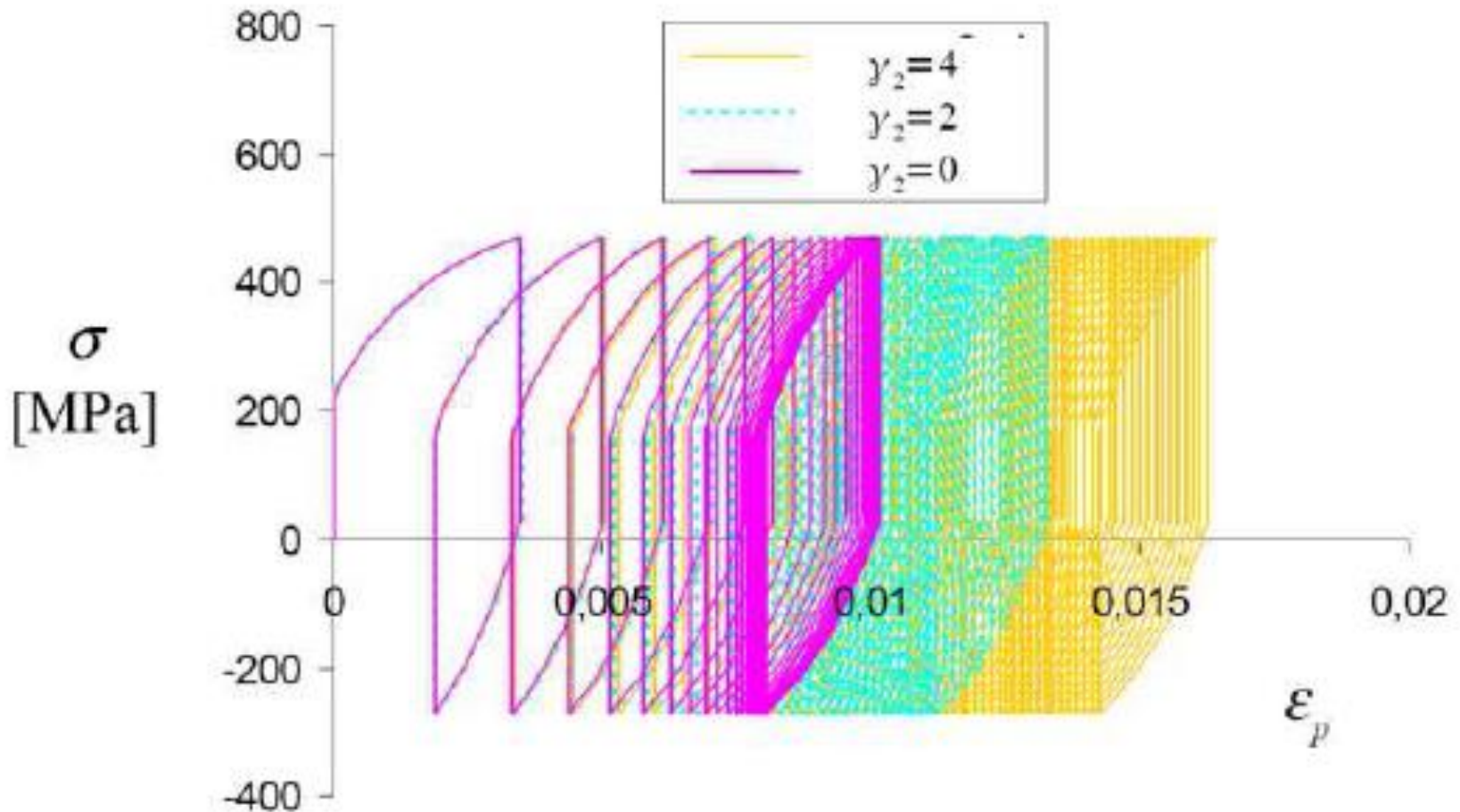


Fig. 17

## hardening Models

Occurrence of cyclic plasticity models in some popular FE software

<b>Kinematic hardening</b>	<b>Ansys 13</b>	<b>Abaqus</b>	<b>MSC.Marc</b>	<b>MSC. Nastran</b>
<i>Bilinear</i>	x (Prager)	x	x (Ziegler)	x (Ziegler)
<i>Multilinear</i>	x (Besseling)	-	-	-
<i>Armstrong-Frederick</i>	x	x	x	x
<i>Chaboche</i>	x ( $M_{\max}=5$ )	x ( $M_{\max}=3$ )	-	-

## **References:**

- Akhtar S. Khan, S. Huang, ***Continuum Theory of Plasticity***, John Wiley and Sons, 1995.
- Peep Miidla, ***Numerical Modelling***, 2012, InTech Publication.
- Marcio Costa Araújo , ***NON-LINEAR KINEMATIC HARDENING MODEL FOR MULTIAXIAL CYCLIC PLASTICITY, 2002***, Universidade Federal do Piauí, Brazil.
- Koichi Hashiguchi, ***Elastoplasticity Theory, 2009, Springer***,



***"You cannot depend on your eyes when your imagination is out of focus."  
Mark Twain***

