Norman S. Nise CONTROL SYSTEMS ENGINEERING

Seventh Edition



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Norman S. Nise

California State Polytechnic University, Pomona



To my wife, Ellen; sons, Benjamin and Alan; and daughter, Sharon, and their families.

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