

Mathematics for AI

Lecture 1a

Introduction and Logistics

Mathematics for Artificial Intelligence



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University of Technology

- Graduate Course
- 3 credits, 32 sessions
- Saturday, Wednesday, 15:30-17:30
- Instructor: Behrooz Nasihatkan
- Email: nasihatkon@kntu.ac.ir
- Office: Room 402

Exam Dates



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- Midterm Exam: **Thursday, 17 Aban, 9:00-12:00**
- Final Exam: look at the schedule

Ask Questions



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Special Needs



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Eating in class



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How to get help



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How to give feedback?



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Anonymous form: <https://goo.gl/zPxBAS>



Join the Telegram channel



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https://t.me/math4AI_4021



My Telegram Channel



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t.me/behrooznasihatkon



What is considered cheating?



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- Homework



Why this course?

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Why this course?



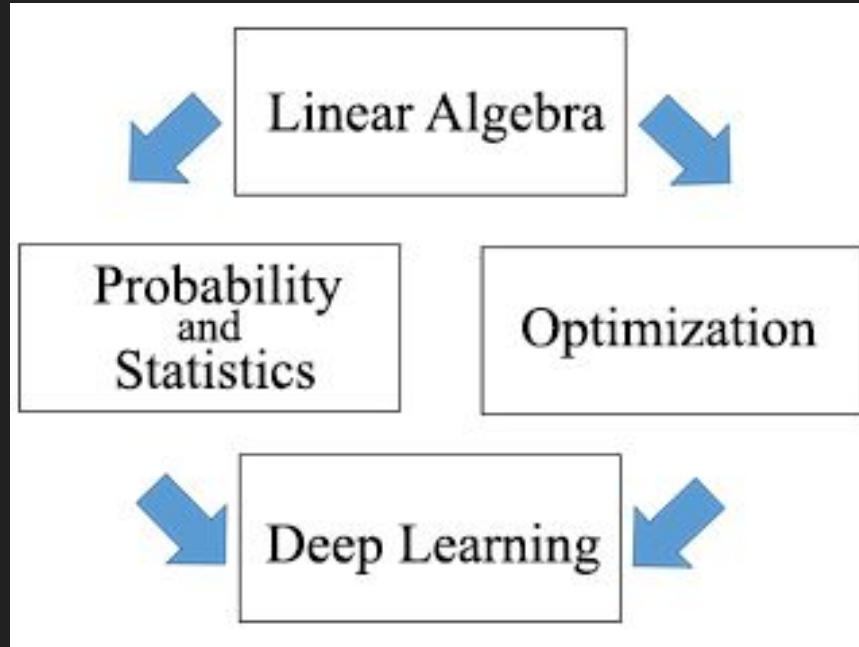
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Why this course?



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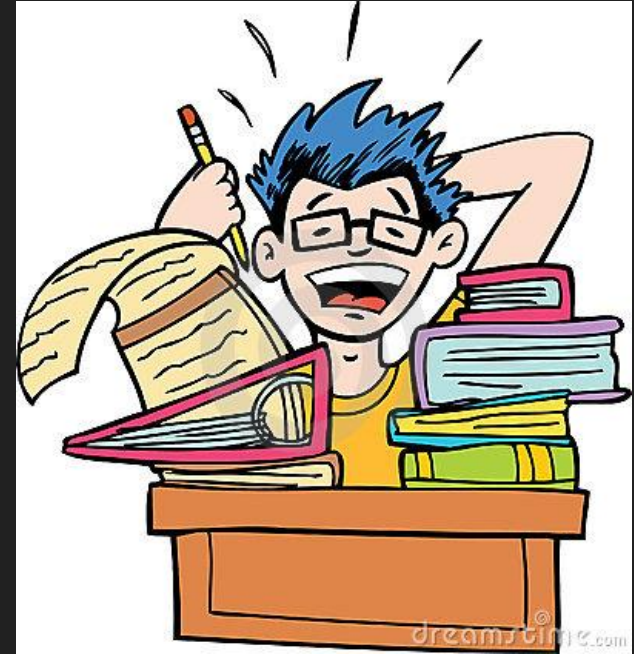
<https://ocw.mit.edu/courses/18-065-matrix-methods-in-data-analysis-signal-processing-and-machine-learning-spring-2018/>

Evaluation

- Lab Sessions
- Homework
- Projects
- Midterm Exam
- Final Exam



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Programming Languages



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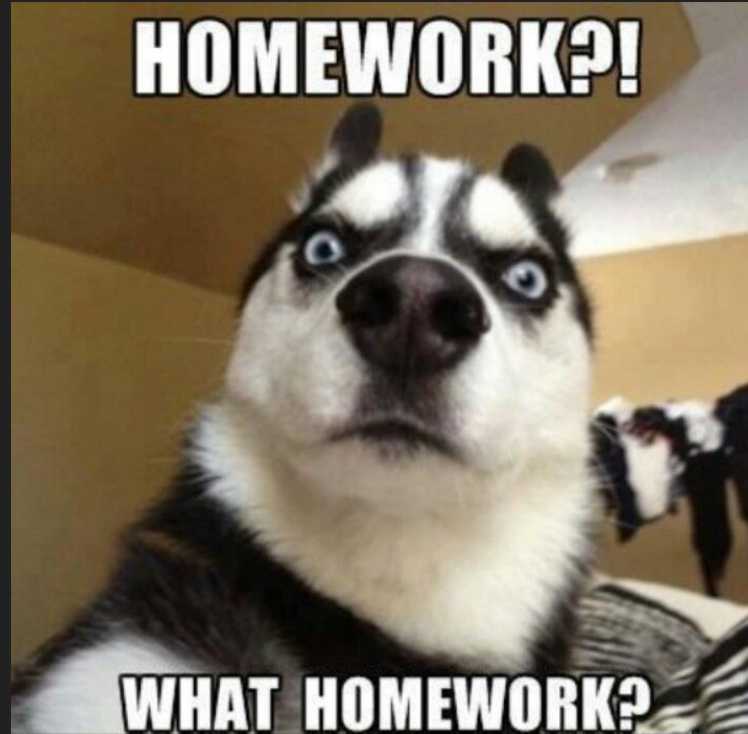
- Matlab
- C++
- **Python**
- R
- Julia
- ...

Homework/Projects



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Labs



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Linear Algebra Libraries

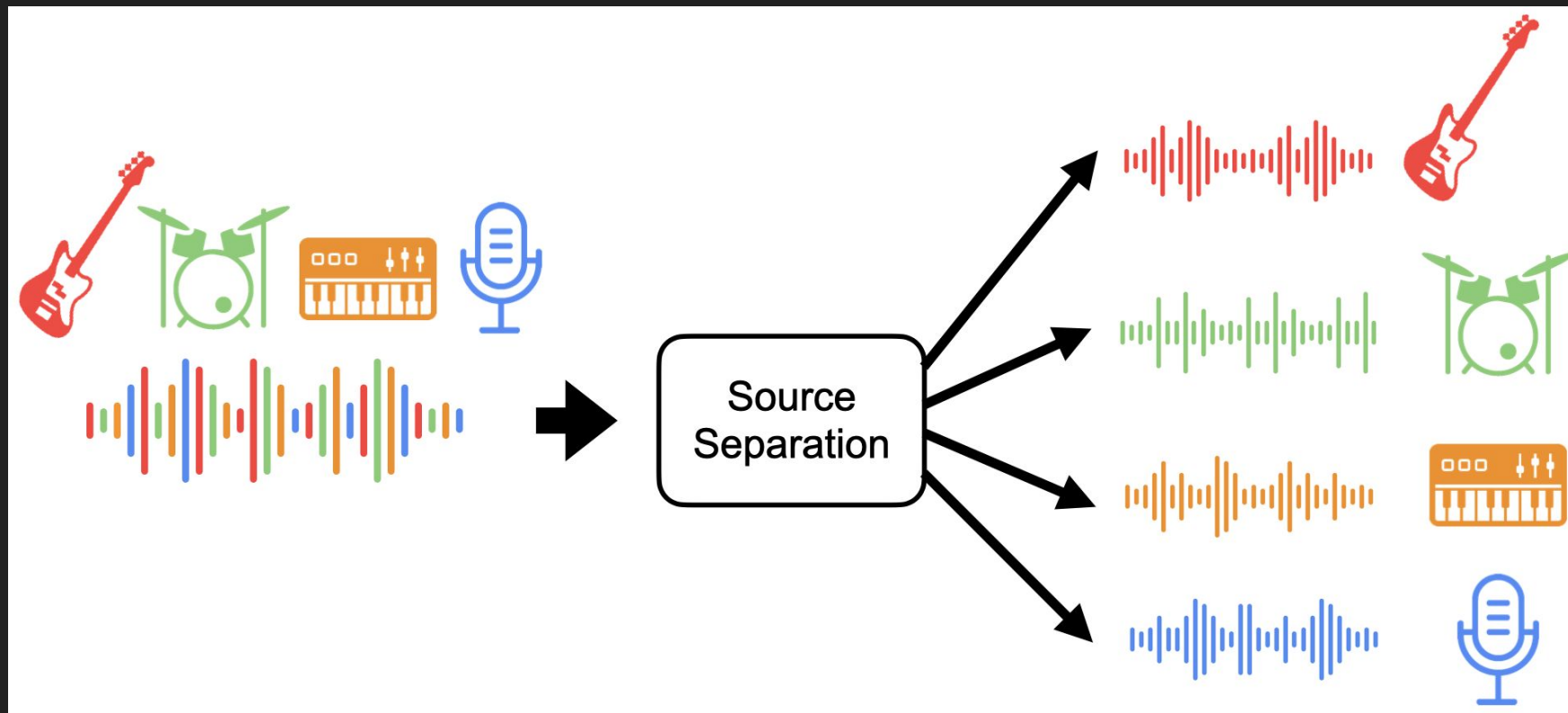


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- BLAS implementations (OpenBLAS, BLIS, Intel MKL, cuBLAS)
- Llapack
- Eigen
- Python/Numpy (numpy.linalg, scipy.linalg)
- TensorX

- Look:
 - https://en.wikipedia.org/wiki/List_of_numerical_libraries
 - https://en.wikipedia.org/wiki/Comparison_of_linear_algebra_libraries

Example: Source Separation



Source Separation



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<https://youtu.be/n7y2rLAnd5I>

Source Separation



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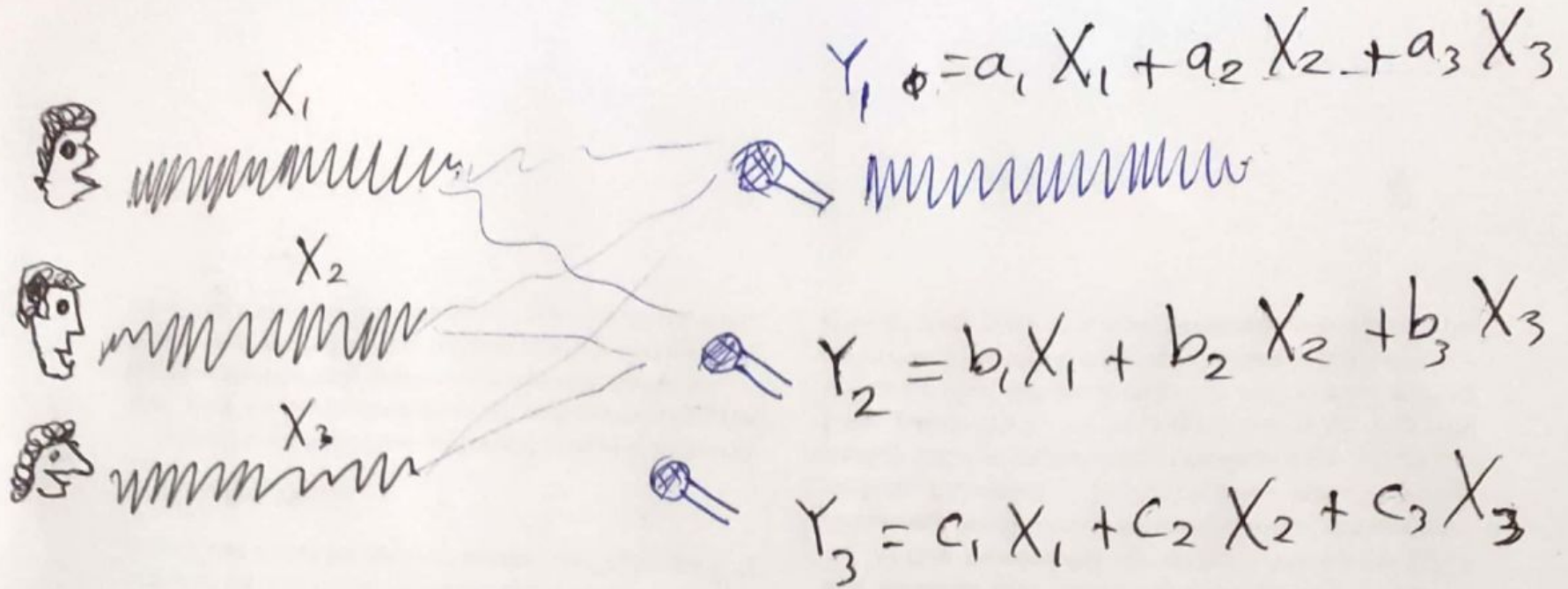


<https://www.youtube.com/watch?v=tkkm6zVUDXo>

Example: Source Separation



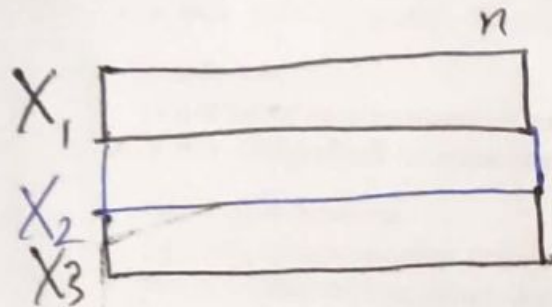
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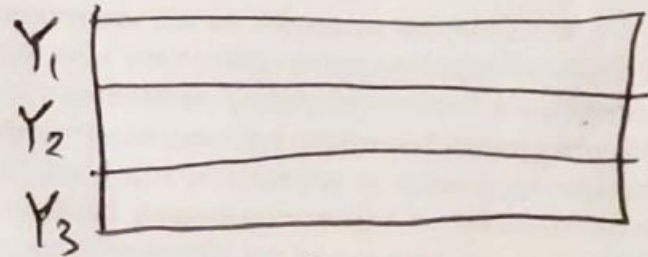
Example: Source Separation



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$$X = \begin{bmatrix} X_1 \\ X_2 \\ X_3 \end{bmatrix} \in \mathbb{R}^{3 \times n}$$



$$Y = \begin{bmatrix} Y_1 \\ Y_2 \\ Y_3 \end{bmatrix} \in \mathbb{R}^{3 \times n}$$

Example: Source Separation



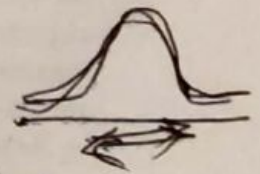
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$$\begin{matrix} Y_1 \\ Y_2 \\ Y_3 \end{matrix} \begin{matrix} \bigcirc \\ \\ \\ \end{matrix} \begin{matrix} \\ \\ \\ \end{matrix} = \begin{bmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{bmatrix} \begin{bmatrix} \bigcirc & \bigcirc \\ \bigcirc & \bigcirc \\ \bigcirc & \bigcirc \end{bmatrix} \begin{matrix} X_1 \\ X_2 \\ X_3 \end{matrix}$$

Y A X

blind source separation

A
 $B B^T$



Example: Source Separation



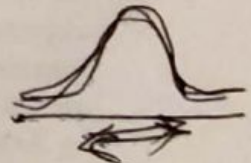
blind source separation

$$Y = A X \Rightarrow X = A^{-1} Y$$

$3 \times n$ 3×3 $3 \times n$

Independent Component Analysis (ICA) $\int p(a) \log(p(a))$

$$Y = A' X' = (A' B) (B^{-1} X')$$





Example: Source Separation

- Linear Algebra:

$$Y = A X \Rightarrow X = A^{-1} Y$$

- Probability and Statistics:

$$\text{Entropy} = - \int p(x) \log(p(x)) dx$$

- Optimization

$$\min_{A, X} \text{Entropy}(X) \text{ subject to } Y = A X$$