

Modeling of a special physical phenomenon results into the following system of equations:

 $x_{i-1} - 2x_i + x_{i+1} = i \times ab$

in which ab is the first two digits of your *Student ID*, after removing it's first three digits. For example, if *Sdutent ID* = 9107532 then ab = 75. In this problem, x_0 is always equal to zero; i.e. $x_0 = 0$ and $x_n = CN$; where CN is your class number. Suppose that we want to solve a 5 × 5 system of equations (Note that i = 0 and i = 6 are known and i = 1 to i = 5 are unknown)

- 1. Make the system of equations and write it down in compact form.
- 2. Obtain the *Gauss Elimination* subroutine form *Numerical Recipes* and solve the problem.
- 3. Obtain the inverse of the matrix using *Gauss Elimination* method.
- 4. Determine the *Condition Number* of your system.
- 5. Solve the system using *Jacobi*, *Gauss–Seidel* and *SOR* methods.